

Ab-initio Description of Strongly-Correlated Materials

Basics of DFT+DMFT

Markus Aichhorn

Institute of Theoretical and Computational Physics



The standard model: Density Functional Theory (DFT)



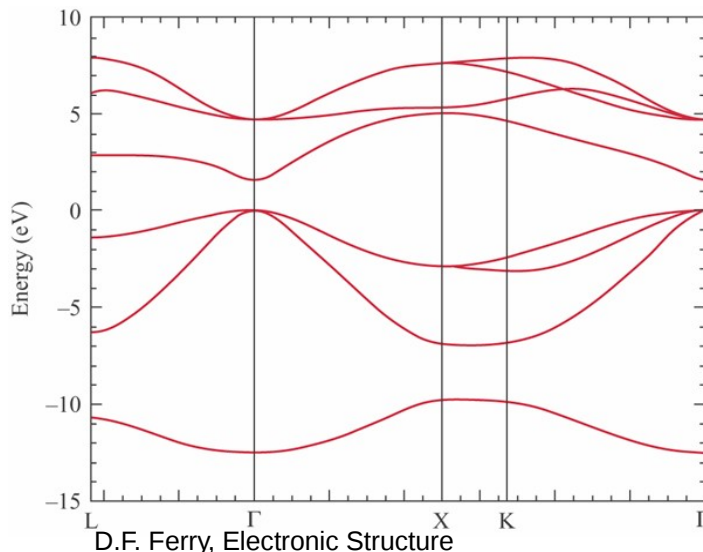
Walter Kohn
Nobel prize 98

„Ground state density determines all ground state properties“

No need for the wave function \longrightarrow tremendous advantage

Minimisation of energy functional $E = E[\rho]$ determines ρ_0

\longrightarrow Kohn Sham equation / bands



GaAs band structure:

Empty conduction bands

Filled valence bands

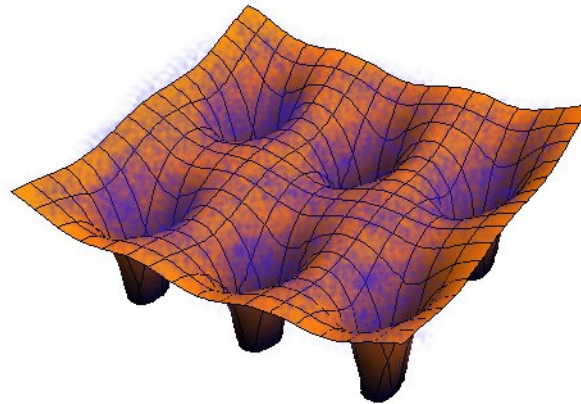
\longrightarrow Semiconductor (Band Insulator)

Nice agreement with real life

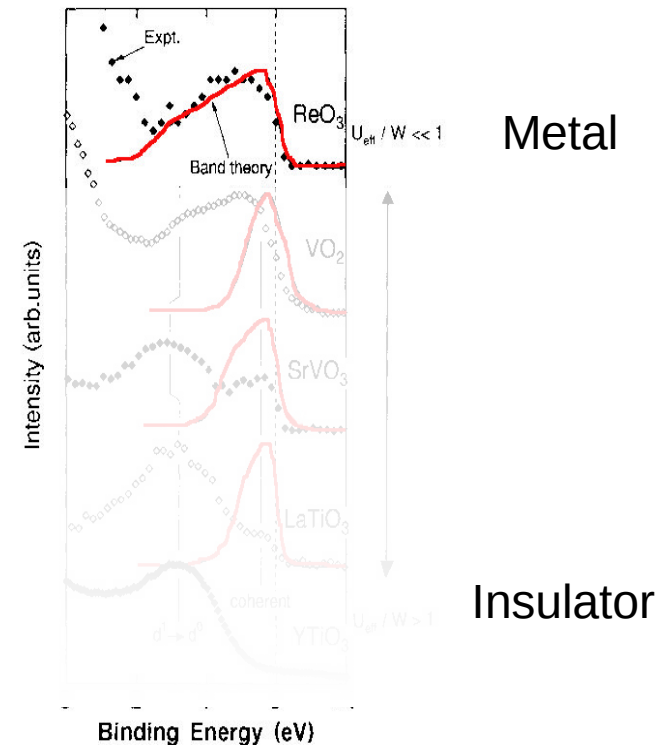
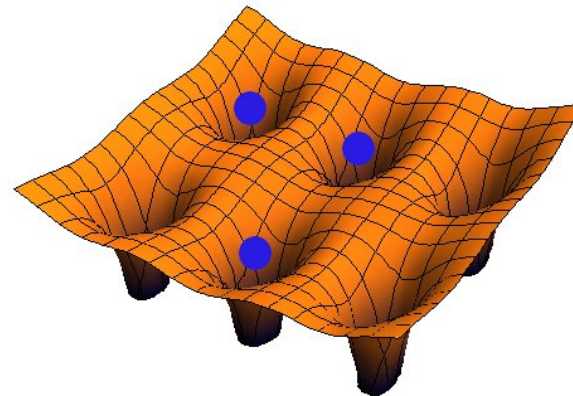


Electronic correlations

Band Theory



Localisation



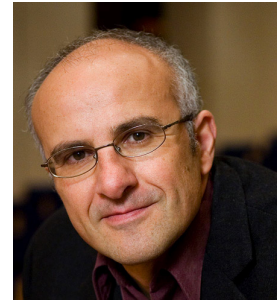
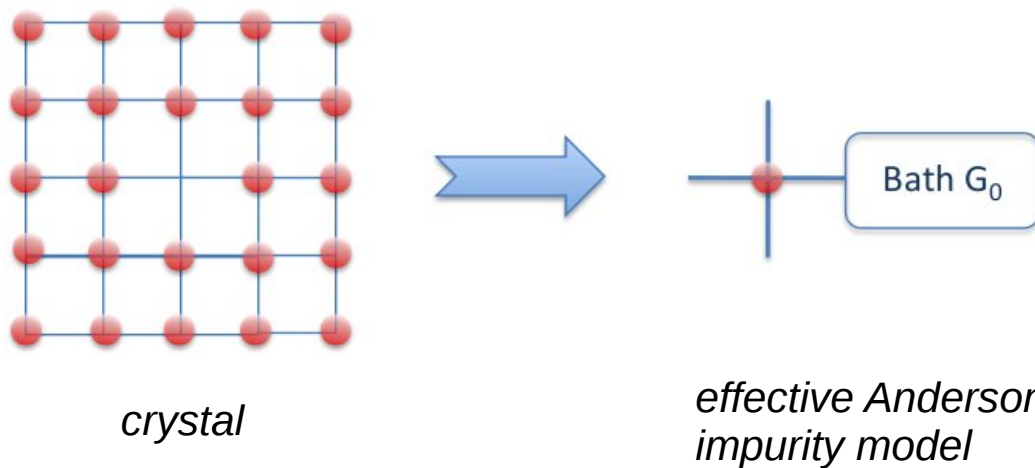
Fujimori, PRL 69, 1796 (1992)

Standard Band Theory fails!

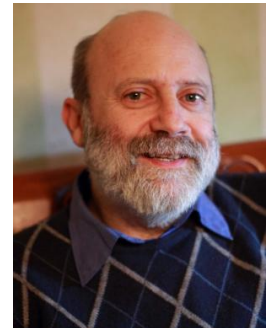


Local Correlations: Dynamical Mean-Field Theory

Replace full system by single atom in effective bath



Antoine Georges



Gabi Kotliar

Atomic physics (local quantum fluctuations) is treated exactly

Mean-field approach: Effective bath determined self-consistently

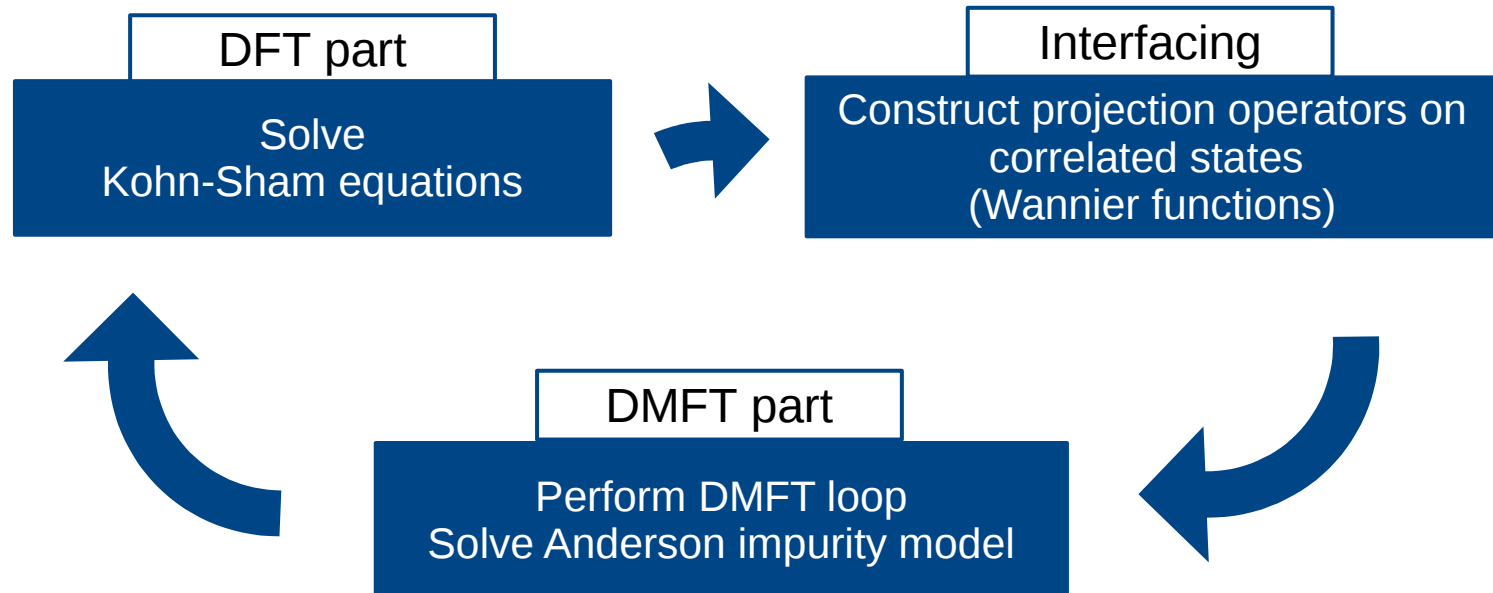
Describes Mott metal-to-insulator transitions

A. Georges *et al.*, RMP 1996



Ab initio description: DFT + DMFT

Combine band theory (DFT) and include local atomic correlations (DMFT)



Self consistent implementation in Wien2K:

Projective Technique: [M. Aichhorn](#) et al., PRB 80, 085101 (2009)

Charge self consistency: [M. Aichhorn](#) et al., PRB 84, 054529 (2011)

Lichtenstein *et al.* 1998; Anisimov *et al.* 1997, G. Kotliar et al., RMP 2006



Multiorbital atomic physics matters

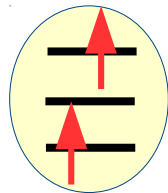
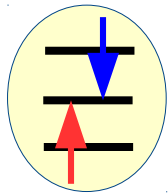
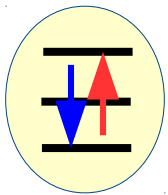
Band theory: Electrons are waves

$$\psi_{\mathbf{k}}(\mathbf{r}) = e^{i\mathbf{k}\mathbf{r}} u_{\mathbf{k}}(\mathbf{r})$$

Mott Insulator: Electrons localize!



Atomic structure becomes important!



$$U \sum_{\alpha} n_{\alpha\uparrow} n_{\alpha\downarrow}$$

$$U' \sum_{\alpha \neq \beta} n_{\alpha\uparrow} n_{\beta\downarrow}$$

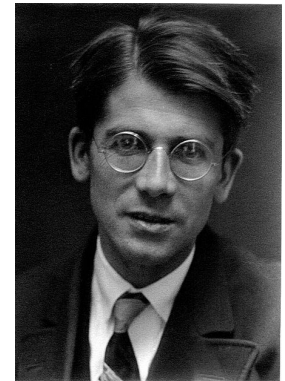
$$(U' - J) \sum_{\alpha \neq \beta} n_{\alpha\uparrow} n_{\beta\uparrow}$$

Atomic Hamiltonian

describes local physics

Important ingredient:

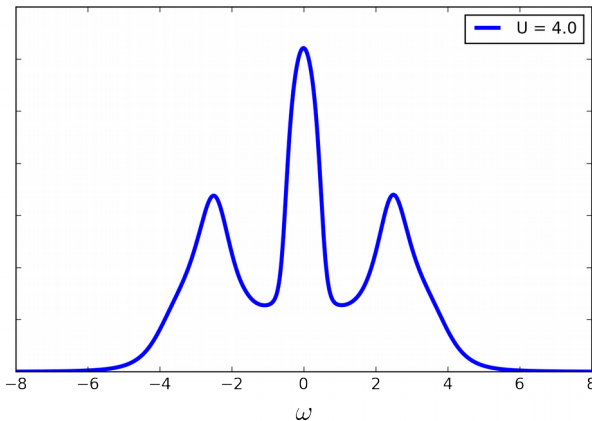
Hund's rule coupling



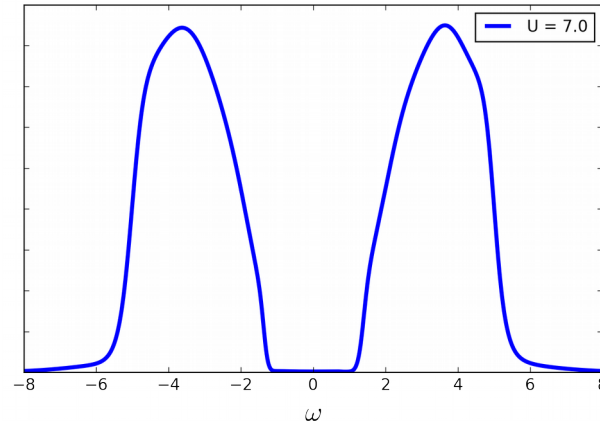
Friedrich Hund



Local Correlations: Dynamical Mean-Field Theory



Correlated metal



Insulator

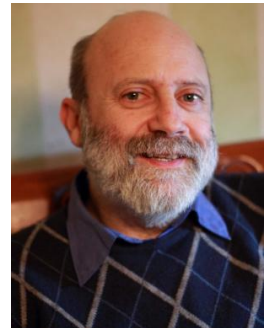
DMFT solution for the single-orbital Hubbard model

Exact Limiting cases:

- Noninteracting Electrons
- Atomic limit
- Infinite dimension / coordination



Antoine Georges



Gabi Kotliar

A. Georges *et al.*, RMP 1996



triqs

a Toolbox for Research on Interacting Quantum Systems

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Welcome

TRIQS (Toolbox for Research on Interacting Quantum Systems) is a scientific project providing a set of C++ and Python libraries to develop new tools for the study of interacting quantum systems.

The goal of this toolkit is to provide high level, efficient and simple to use libraries in C++ and Python, and to promote the use of modern programming techniques.

TRIQS is free software distributed under the GPL license.

TRIQS applications

Based on the TRIQS toolkit, several [full-fledged applications](#) are also available. They allow for example to solve a generic quantum impurity model or to run a complete LDA+DMFT calculation.

Developed in a collaboration between IPHT Saclay and Ecole Polytechnique since 2005, the TRIQS library and applications have allowed us to address questions as diverse as:

- Momentum-selective aspects on cuprate superconductors (with various cluster DMFT methods)
- Degree of correlation in iron-based superconductors (within an LDA+DMFT approach)
- Fermionic Mott transition and exploration of Sarma phase in cold-atoms


Python & C++

The libraries exist at two complementary levels: on the one hand, C++ libraries allow to quickly develop high-performance low-level codes; on the other hand python libraries implement the most common many-body objects, like Green's functions, that can be manipulated easily in python scripts.

This duality is a real advantage in the development of new many-body tools. Critical parts where performance is essential can be written in C++ (e.g. a quantum impurity solver) while the data analysis, preparation of the inputs or interface with other programs can be done at the very user-friendly python level.

TRIQS 1.3

This is the homepage of the TRIQS release 1.3. For the changes in 1.3, Cf [changelog page](#)



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M. Aichhorn *et al.*, CPC 204, 200–208 (2016)
 O. Parcollet *et al.*, CPC 196, 398–415 (2015)